

**GOVERNMENT OF KARNATAKA
DEPARTMENT OF PRE-UNIVERSITY EDUCATION
II YEAR PUC SUPPLEMENTARY EXAMINATION – AUGUST 2022
SCHEME OF VALUATION**

Subject code: 31(NS)

Subject: STATISTICS

Q. NO.	I. SECTION – A	MARKS
1.	$P_t = P_0 + (B - D) + (I - E)$	1
2.	Expected number of years that a new born baby would live.	1
3.	Paasche's index number.	1
4.	The index number of the cost met by a specified class of consumers in buying a 'basket of goods and services'.	1
5.	Time series helps in planning and forecasting the business activities. (Any one)	1
6.	Irregular / random / erratic variation.	1
7.	Mean = 0.6	1
8.	Median = 12.34	1
9.	$-\infty < t < \infty$	1
10.	The set of all the admissible values of the parameters.	1
11.	Method of obtaining the most likely value of the parameter using statistic.	1
12.	d. f. = 1	1
13.	np – chart (d-chart) or c- chart. (Any one)	1
14.	If $v = 0$.	1
15.	Profit due to increasing market price. (Any one)	1

Q.NO.	II. SECTION - B	MARKS												
16.	$\text{IMR} = \frac{\text{Number of deaths among infants in the year}}{\text{Total number of live births in the year}} \times 1000$ $= 60$	1 1												
17.	Life tables are used by life insurance companies. Life table is used for estimating the future population. (Any two)	1 1												
18.	$P_{01}^{(DB)} = \frac{P_{01}(L) + P_{01}(P)}{2}$ $= 250$	1 1												
19.	$V_{01} = \frac{\sum p_1 q_1}{\sum p_0 q_0} \times 100$ $= 125$	1 1												
20.	(i) Defining purpose and scope. (ii) Obtaining price quotations. (Any two)	1 1												
21.	(i) Prosperity (ii) Decline (Recession) (iii) Depression (iv) improvement (Recovery)	1 1												
22.	Merit: The method is mathematical and so, it is highly efficient. (Any one) Demerit: The procedure of calculation is difficult. (Any one)	1 1												
23.	Interpolation is the technique of estimating the value of dependent variable for any intermediate value of the independent variable. Extrapolation is the technique of estimating the value of dependent variable for any value of the independent variable which is outside the given range.	1 1												
24.	$\text{S.D.} = \sqrt{pq}$ $= 0.477$	1 1												
25.	$\text{Variance} = 2n$ $= 22$	1 1												
26.	$\text{S.E.}(p) = \sqrt{\frac{PQ}{n}}$ $= 0.05$	1 1												
27.	Null hypothesis is the hypothesis which is being tested for a possible rejection, under the assumption that it is true. Alternative hypothesis is the hypothesis which is accepted when null hypothesis is rejected.	1 1												
28.	$\text{L.C.L.} = \bar{c} - 3\sqrt{\bar{c}}$ $= -2$	1 1												
29.	<p style="text-align: center;">Player - A</p> <table style="margin-left: auto; margin-right: auto;"> <tr> <td></td> <td>A₁</td> <td>A₂</td> <td>A₃</td> </tr> <tr> <td>Player - B</td> <td>B₁ [5</td> <td>3</td> <td>-1]</td> </tr> <tr> <td></td> <td>B₂ [4</td> <td>2</td> <td>-2]</td> </tr> </table>		A ₁	A ₂	A ₃	Player - B	B ₁ [5	3	-1]		B ₂ [4	2	-2]	1 1
	A ₁	A ₂	A ₃											
Player - B	B ₁ [5	3	-1]											
	B ₂ [4	2	-2]											
30.	Controlled variables. Uncontrolled variables.	1 1												

Q.NO.	III. SECTION – C	MARKS
31.	$\text{ASFR} = \frac{\text{Number of Live births in a specified age group in a year}}{\text{Total number of females in that particular age group in a year}} \times 1000$ ASFRs : 20 120 180 125 30 8 4 Total: 487 $\text{TFR} = 5 \times \Sigma \text{Quinquennial ASFRs}$ $= \mathbf{2435}$	1 2 1 1
32.	$\text{WSFR} = \frac{\text{No.of Female births in a specified age group in a year}}{\text{Total no.of females in that particular age group in a year}} \times 1000$ WSFR: 20 30 60 40 30 20 10 WSFR X S: 18 27 54 34 24 16 7 $\Sigma \text{WSFR X S} = \mathbf{180}$ $\text{NRR} = i \times \Sigma \text{WSFR X S}$ $= \mathbf{900}$	1 1 1 1
33.	1. Index number simplifies the data thus facilitates comparative study. } (Any 2. Index numbers are used in studying trends and tendencies. } three 3. Index numbers help in measuring purchasing power of money. } Uses) 1. Many formulae are used in the construction of index numbers } (Any and the different formulae give different answers. } two 2. While constructing index numbers, the quality of the product is } limitations) not taken into consideration. }	1 1 1 1 1
34.	$P = \frac{P_1}{P_0} \times 100$ P: 110 160 115 105 120 WP: 3850 2400 2300 1050 2400 $\Sigma \text{WP} = \mathbf{12000}$ $\text{CPI} = \frac{\Sigma \text{WP}}{\Sigma W}$ $\text{CPI} = \mathbf{120}$	1 1 1 1 1
35.	3-yearly moving sums: - 120 120 129 141 150 156 165 - 3-yearly moving averages: - 40 40 43 47 50 52 55 - Position of trend values. Conclusion: The given data shows upward trend.	2 1 1 1
36.	Table and $n = 5$, $\Sigma y = 515$, $\Sigma x = 0$, $\Sigma x^2 = 10$, $\Sigma xy = 179$ $a = \frac{\Sigma y}{n} = \frac{515}{5} = \mathbf{103}$ $b = \frac{\Sigma xy}{\Sigma x^2} = \frac{179}{10} = \mathbf{17.9}$ The trend equation is, $y = 103 + 17.9(x)$	2 1 1 1
37.	5 12 19 26 - 40 - $(y_0) (y_1) (y_2) (y_3) (y_4) (y_5) (y_6)$ $(y - 1)^5 = 0 \Rightarrow y_5 - 5y_4 + 10y_3 - 10y_2 + 5y_1 - y_0 = 0$ $y_4 = \mathbf{33}$ tons $y_6 - 5y_5 + 10y_4 - 10y_3 + 5y_2 - y_1 = 0$ $y_6 = \mathbf{47}$ tons	1 1 1 1 1
38.	$p(x) = {}^6C_x (0.4)^x (0.6)^{6-x}, x = 0,1,2,3,4,5,6$ a) $P(X = 3) = {}^6C_3 (0.4)^3 (0.6)^{6-3}$ $= \mathbf{0.2765}$ b) $P(X \geq 1) = 1 - p(0) = 1 - q^n$ $= \mathbf{0.9533}$	1 1 1 1 1

39.	$P(X=2) = \frac{{}^6C_2 \cdot {}^9C_{4-2}}{15C_4}$ $= \mathbf{0.3956}$ $\text{S.D.}(X) = \sqrt{\frac{nab(a+b-n)}{(a+b)^2(a+b-1)}}$ $= \sqrt{\frac{4 \times 6 \times 9 (11)}{225(14)}}$ $= \mathbf{0.8685}$	1 1 1 1
40.	$H_0: \mu_1 = \mu_2 \quad \text{and} \quad H_1: \mu_1 \neq \mu_2$ $Z_{\text{cal}} = \frac{\bar{x}_1 - \bar{x}_2}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$ $= \mathbf{1.8488}$ $k = \pm 1.96$ $\therefore H_0 \text{ is accepted.}$	1 1 1 1
41.	$H_0: \mu = 35 \quad \text{and} \quad H_1: \mu > 35$ $t_{\text{cal}} = \frac{\bar{x} - \mu_0}{s/\sqrt{n-1}}$ $= \mathbf{1.3333}$ $k = 1.75$ $\therefore H_0 \text{ is accepted.}$	1 1 1 1
42.	$H_0: \sigma^2 = 100 \quad \text{and} \quad H_1: \sigma^2 < 100$ $\chi^2_{\text{cal}} = \frac{ns^2}{\sigma_0^2}$ $= \mathbf{16.2}$ $k_1 = 7.63$ $\therefore H_0 \text{ is accepted.}$	1 1 1 1
43.	$CL = \bar{R} = \mathbf{6}$ $LCL = D_3\bar{R}$ $= \mathbf{0}$ $UCL = D_4\bar{R}$ $= \mathbf{13.692}$	1 1 1 1
44.	<p>Co-ordinates: (0,4), (10,0) and (0,7), (7,0) Drawing two lines. Identification of F.R. and its corner points: A(0,4), B(0,7), C(5,2) Objective function values: $Z_A = 12$, $Z_B = 21$, $Z_C = 46$. Maximum value of $Z = \mathbf{46}$ and optimal solution: $x = \mathbf{5}$ & $y = \mathbf{2}$</p> <p>(For visually challenged students only)</p> <p>Steps for solving LPP graphically.</p>	1 1 1 1 1 5
45.	NWCR method and $x_{11} = 80$ $x_{12} = 150$ $x_{13} = 120$ $x_{23} = 110$ $x_{33} = 100$ Transportation cost = Rs 5170	3 2

Q. NO.	IV. SECTION – D	MARKS
46.	$\text{ASDR} = \frac{\text{Number of deaths in a specific age group in a year}}{\text{Total population in that age group in a year}} \times 1000$ ASDR(A): 10 5 15 21 ASDR(B): 11 4 12 20 PA: 1,50,000 1,25,000 6,00,000 2,10,000 $\Sigma \text{PA} = 10,85,000$ PB: 1,65,000 1,00,000 4,80,000 2,00,000 $\Sigma \text{PB} = 9,45,000$ $\Sigma \text{P} = 90,000$ $\text{STDR}_A = \frac{\Sigma \text{PA}}{\Sigma \text{P}}$ and $\text{STDR}_B = \frac{\Sigma \text{PB}}{\Sigma \text{P}}$ $\text{STDR}(A) = 12.06$ $\text{STDR}(B) = 10.5$ Interpretation: Locality B is healthier.	1 1 1 1 1 1 1 1 1 1
47.	p_0q_0 : 60 100 60 10 45 $\Sigma p_0q_0 = 275$ p_0q_1 : 100 150 90 20 30 $\Sigma p_0q_1 = 390$ p_1q_0 : 75 120 50 8 30 $\Sigma p_1q_0 = 283$ p_1q_1 : 125 180 75 16 20 $\Sigma p_1q_1 = 416$ $P_{01}^{(L)} = \frac{\Sigma p_1q_0}{\Sigma p_0q_0} \times 100$ $= 102.9$ $P_{01}^{(P)} = \frac{\Sigma p_1q_1}{\Sigma p_0q_1} \times 100$ $= 106.67$ $P_{01}^{(F)} = \sqrt{P_{01}^{(L)} \times P_{01}^{(P)}}$ $= 104.77$	1 1 1 1 1 1 1 1
48.	p_0q_0 : 50 120 10 40 $\Sigma p_0q_0 = 220$ p_0q_1 : 70 180 25 48 $\Sigma p_0q_1 = 323$ p_1q_0 : 60 126 12 40 $\Sigma p_1q_0 = 238$ p_1q_1 : 84 189 30 48 $\Sigma p_1q_1 = 351$ $P_{01}^{(ME)} = \frac{\Sigma p_1q_0 + \Sigma p_1q_1}{\Sigma p_0q_0 + \Sigma p_0q_1} \times 100$ $= \frac{238 + 351}{220 + 323} \times 100 = \frac{589}{543} \times 100$ $= 108.47$ According to TRT, $P_{01} \times P_{10} = 1$ $P_{01}^{ME} \times P_{10}^{ME} = \frac{\Sigma p_1q_0 + \Sigma p_1q_1}{\Sigma p_0q_0 + \Sigma p_0q_1} \times \frac{\Sigma p_0q_1 + \Sigma p_0q_0}{\Sigma p_1q_1 + \Sigma p_1q_0}$ $= \frac{238 + 351}{220 + 323} \times \frac{323 + 220}{351 + 238} = \frac{589}{543} \times \frac{543}{589} = 1$	1 1 1 1 1 1 1 1
49.	$\Sigma x = 0$, $\Sigma x^2 = 70$, $\Sigma \log y = 6.681$, $\Sigma x \log y = 3.4336$ $\log a = \frac{\Sigma \log y}{n} = 1.1135$ $\log b = \frac{\Sigma x \log y}{\Sigma x^2} = 0.049$ $\log y = 1.1135 + 0.049x$ $\hat{y}_{2021} = 28.61$ Lakhs	1+1+1+1 1+1 1+1 1 1
50. a	$n = 4$, $N = 128$, $p = 0.5$ and $q = 0.5$ $p(0) = q^n = 0.0625$ or $T(0) = N \times p(0) = 8$ $T(1) = 32$ $T(2) = 48$ $T(3) = 32$ $T(4) = 8$	1 1 3
50. b	H_0 : Poisson distribution is a good fit H_1 : Poisson distribution is not a good fit $\chi_{cal}^2 = \sum \frac{(O-E)^2}{E}$ $= 1.2432$ $k_2 = 5.99$ $\therefore H_0$ is accepted.	1 1 1 1 1

Q. NO.	V. SECTION – E	MARKS
51.	$\mu = 80, \sigma = 5, Z = \frac{x-80}{5}$ is a S.N.V.	1
	a) $P(X > 70) = P(Z > -2)$	1
	$= \mathbf{0.9772}$	1
	b) $P(X < 85) = P(Z < 1)$	1
	$= \mathbf{0.8413}$	1
52.	$H_0 : P_1 = P_2 \quad H_1 : P_1 \neq P_2$	1
	$Z_{cal} = \frac{p_1 - p_2}{\sqrt{PQ(\frac{1}{n_1} + \frac{1}{n_2})}}$	1
	$= \mathbf{0.789}$	1
	$k = \pm 1.96$	1
	$\therefore H_0$ is accepted.	1
53.	$H_0 : \mu_1 = \mu_2 \quad H_1 : \mu_1 < \mu_2$	1
	$t_{cal} = \frac{\bar{d}}{S_d / \sqrt{n-1}}$	1
	$= \mathbf{-1.943}$	1
	$k = - 3.75$	1
	$\therefore H_0$ is accepted.	1
54.	$P - S_n = 5000$	1
	$\Sigma C_i : 200 \quad 550 \quad 1000 \quad 1600 \quad 2500 \quad 4300$	1
	$T(n) : 5200 \quad 5550 \quad 6000 \quad 6600 \quad 7500 \quad 9300$	1
	$A(n) : 5200 \quad 2775 \quad 2000 \quad 1650 \quad \mathbf{1500} \quad 1550$	1
	\therefore The optimum replacement period, $n = \mathbf{5}$ years.	1
55.	$R = 12000 \quad C_1 = 10 \quad C_3 = 300$	1
	a) $Q^0 = \sqrt{\frac{2C_3R}{C_1}}$	1
	$= \mathbf{848.52}$ units.	1
	b) $C(Q^0, S^0) = \sqrt{2C_1C_3R}$	1
	$= \mathbf{Rs 8485.28}$ /year.	1
